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15CS/IS54

## Fifth Semester B.E. Degree Examination, June/July 2019 Automata Theory and Computability

Time: 3 hrs.

Max. Marks: 80

**Note: Answer any FIVE full questions, choosing ONE full question from each module.**

### Module-1

- 1 a. Define the following : i) string ii) alphabet iii) language. (06 Marks)
- b. Design a deterministic finite state machine for the following language over  $\Sigma = \{a, b\}$ .
  - i)  $L = \{W \mid |W| \bmod 3 > |W| \bmod 2\}$
  - ii)  $L = \{w \mid W \text{ ends either with } ab \text{ or } ba\}$ . (10 Marks)

OR

- 2 a. Write a note on finite state transducers. (07 Marks)
- b. Define DFSM? Minimize the following FSM. [Refer Fig.Q2(b)]

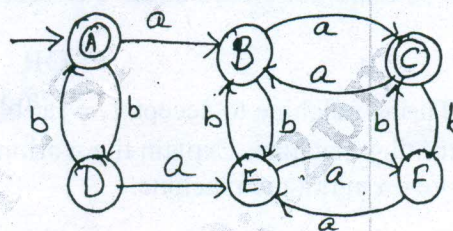


Fig.Q2(b)

(09 Marks)

### Module-2

- 3 a. Write the equivalent Regular Expression for the given Finite state machine. [Refer Fig.Q3(a)] (08 Marks)

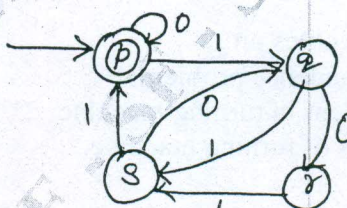


Fig Q3(a)

- b. Write the Regular Expression for the following language.
  - i)  $\{w \in \{a, b\}^* \text{ with atmost one } a\}$
  - ii)  $\{w \in \{a, b\}^* \text{ does not end with } ba\}$
  - iii)  $\{w \in \{0, 1\}^* \text{ has substring } 001\}$
  - iv)  $\{w \in \{0, 1\}^* \mid |W| \text{ is even}\}$ . (08 Marks)

OR

- 4 a. State and prove the pumping theorem for regular language. (08 Marks)
- b. Show that the language  $L = \{a^n b^n \mid n \geq 0\}$  is not regular. (08 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.  
2. Any revealing of identification, appeal to evaluator and /or equations written eg, 42+8 = 50, will be treated as malpractice.





**Module-3**

- 5 a. Define grammar. Write the CFG for the following language.
- i)  $L = \{w \in \{a, b\}^* \mid n_a(w) = n_b(w)\}$
  - ii)  $L = \{a^i b^j \mid i = j + 1\}$ . (08 Marks)
- b. What is inherent ambiguity? Show that the language given is inherently ambiguous?
- $L = \{a^n b^n c^m \mid n, m \geq 0\} \cup \{a^n b^m c^n \mid n, m \geq 0\}$ . (08 Marks)

OR

- 6 a. Define PDA? Design PDA for the language  $L = \{a^n b^m a^n \mid n, m \geq 0\}$ . (06 Marks)
- b. Convert the following language from CFG to PDA  $L = \{ww^R \mid w \in \{0, 1\}^*\}$ . (06 Marks)
- c. Convert the following CFG to CNF  $E \rightarrow E + E \mid E * E \mid (E) \mid id$ . (04 Marks)

**Module-4**

- 7 a. Prove that the language  $L = \{a^n b^n c^n \mid n \geq 0\}$  is not context free. (08 Marks)
- b. Prove that CFL are not closed under intersection, complement or difference? (08 Marks)

OR

- 8 a. Design a Turing machine to accept  $L = \{a^n b^n c^n \mid n \geq 0\}$ . (08 Marks)
- b. Define a turning machine. Explain the working of a turning machine. (05 Marks)
- c. Write a note on multitape machine. (03 Marks)

**Module-5**

- 9 Write a short notes on :
- a. Growth rate of function (05 Marks)
  - b. Church-turning thesis (06 Marks)
  - c. Linear bounded automata. (05 Marks)

OR

- 10 Write a short notes on :
- a. Post correspondence problem (05 Marks)
  - b. Halting problem in turning machine (05 Marks)
  - c. Various types of turning machine. (06 Marks)

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